

| Sr. No. | Content/ Topic | Month & No. of Days | 21 st Century Skills | Learning Objectives | Expected Learn Outcome |
|---------|---------------------------------|--------------------------------|--|--|--|
| 1 | <p>Relations and Functions</p> | March-14 Days | Through problems based on Relations and functions they will Develop: 1)Logical thinking 2)Critical thinking 3)Imagination | To enable the students to understand the role of Relations and Functions Types of relations: reflexive, symmetric, transitive and equivalence relations. One to one and onto and bijective functions. | Students learnt about Equivalence relation, bijective functions. Different types of relations and functions. |
| 2 | Inverse Trigonometric Functions | March-09 Days April-03 Days | Through approach adopted for problems students will attain 1)Imagination 2)Systematic approach | Students will be able to find solutions of problems of inverse trigonometric functions. Inverse trigonometric functions, its domain and range | Students learned about Solutions of problems of inverse trigonometric functions. Inverse trigonometric functions, its domain and range |

$$\begin{aligned} \sin^{-1}(\sin \theta) &= \theta, & \text{for all } \theta \in [-\pi/2, \pi/2] \\ \cos^{-1}(\cos \theta) &= \theta, & \text{for all } \theta \in [0, \pi] \\ \tan^{-1}(\tan \theta) &= \theta, & \text{for all } \theta \in (-\pi/2, \pi/2) \\ \operatorname{cosec}^{-1}(\operatorname{cosec} \theta) &= \theta, & \text{for all } \theta \in [-\pi/2, \pi/2], \theta \neq 0 \\ \sec^{-1}(\sec \theta) &= \theta, & \text{for all } \theta \in [0, \pi], \theta \neq \pi/2 \\ \cot^{-1}(\cot \theta) &= \theta, & \text{for all } \theta \in (0, \pi). \end{aligned}$$

$$\begin{aligned} \sin^{-1}(-x) &= -\sin^{-1}x, x \in [-1, 1] \\ \tan^{-1}(-x) &= -\tan^{-1}x, x \in \mathbb{R} \\ \operatorname{cosec}^{-1}(-x) &= -\operatorname{cosec}^{-1}x, |x| \geq 1 \\ \cos^{-1}(-x) &= \pi - \cos^{-1}x, x \in [-1, 1] \\ \sec^{-1}(-x) &= \pi - \sec^{-1}x, |x| \geq 1 \\ \cot^{-1}(-x) &= \pi - \cot^{-1}x, x \in \mathbb{R} \end{aligned}$$

Inverse Trigonometric Functions

Sum and difference of inverse trigonometric functions

Identities

Properties

Reciprocal identities

- (i) $\sin^{-1}x + \sin^{-1}y = \sin^{-1}(x\sqrt{1-y^2} + y\sqrt{1-x^2})$, where either $x^2 + y^2 \leq 1$ or $xy < 0$.
- (ii) $\sin^{-1}x - \sin^{-1}y = \sin^{-1}(x\sqrt{1-y^2} - y\sqrt{1-x^2})$, where either $x^2 + y^2 \leq 1$ or $xy > 0$.
- (iii) $\cos^{-1}x + \cos^{-1}y = \cos^{-1}(xy - \sqrt{1-x^2}\sqrt{1-y^2})$, if $x + y \leq 0$.
- (iv) $\cos^{-1}x - \cos^{-1}y = \cos^{-1}(xy + \sqrt{1-x^2}\sqrt{1-y^2})$, if $x \leq y$.
- (v) $\tan^{-1}x + \tan^{-1}y = \tan^{-1}\left(\frac{x+y}{1-xy}\right)$, if $xy < 1$.
- (vi) $\tan^{-1}x - \tan^{-1}y = \tan^{-1}\left(\frac{x-y}{1+xy}\right)$, if $xy > -1$.

$$\begin{aligned} \cos^{-1}x &= \sec^{-1}\left(\frac{1}{x}\right) \\ \sin^{-1}x &= \operatorname{csc}^{-1}\left(\frac{1}{x}\right) \\ \tan^{-1}x &= \cot^{-1}\left(\frac{1}{x}\right) \quad (x > 0) \\ &= \cot^{-1}\left(\frac{1}{x}\right) - \pi \quad (x < 0) \end{aligned}$$

Types of Matrices

1. Row matrix

$$(1 \ 2 \ 3)$$

2. Column matrix

$$\begin{bmatrix} 1 \\ 2 \\ 3 \end{bmatrix}$$

3. Rectangular matrix

$$\begin{bmatrix} 1 & 3 & 4 \\ 2 & 5 & 2 \end{bmatrix}$$

4. Square matrix

$$\begin{bmatrix} 1 & 3 & 4 \\ 5 & 2 & 4 \\ 1 & 9 & 6 \end{bmatrix}$$

5. zero matrix

$$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

6. Diagonal matrix

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$$

7. Scalar matrix

$$\begin{bmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 2 \end{bmatrix}$$

8. unit matrix

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

9. upper and lower triangular matrix

$$\begin{bmatrix} 1 & 0 & 0 \\ 2 & 4 & 0 \\ 3 & 5 & 6 \end{bmatrix} \quad \begin{bmatrix} 5 & 8 & 3 \\ 0 & 1 & 2 \\ 0 & 0 & 7 \end{bmatrix}$$

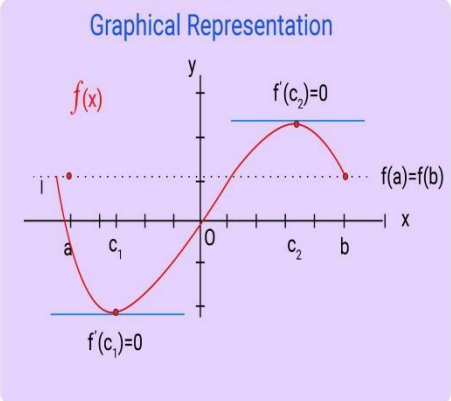
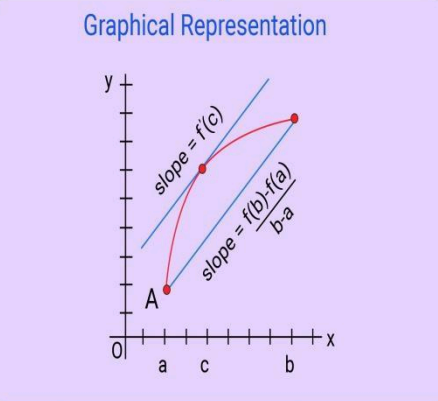
April-15
Days

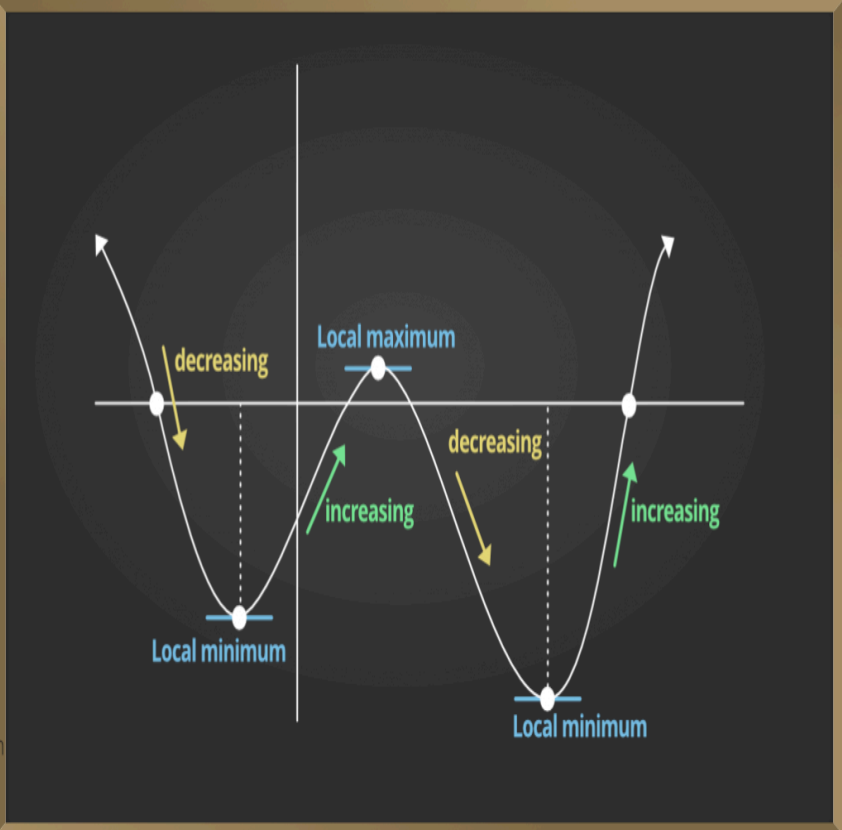
Through problems based on Matrix and Determinants, they will develop
1)Imagination
2)Systematic approach
3)To handle real life situation

Students will be able to learn:
Concept, notation, order, equality, types of matrices, zero and identity matrix, transpose of a matrix, symmetric and skew symmetric matrices.
Operations on matrices: Addition and multiplication and multiplication with a scalar. Simple properties of addition, multiplication and scalar multiplication. Noncommutativity of multiplication of matrices and existence of non-zero matrices whose product is the zero matrix (restrict to square matrices of order 2).

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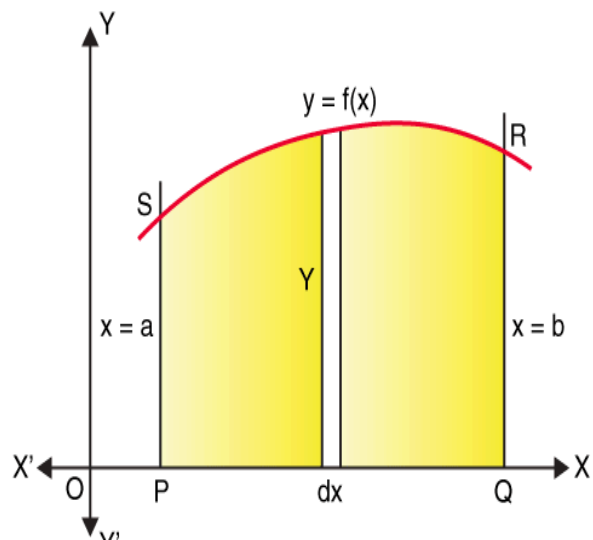
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| 4 | <p style="text-align: center;">Determinants</p> <div style="background-color: #e0f2f1; padding: 5px; border: 1px solid #ccc; margin-bottom: 10px;"> <p>For every square matrix $A = [a_{ij}]$ of order n, we can associate a number called determinant of square matrix. It is denoted by A or $\det(A)$.</p> </div> <h3 style="text-align: center;">Evaluating Determinants</h3> <div style="display: flex; justify-content: space-between;"> <div style="width: 45%;"> <p>(1) Order One: $A = [a]$ $A = a$ $= a$</p> </div> <div style="width: 45%;"> <p>(2) Order Two: $A = \begin{bmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{bmatrix}$ $A = \begin{vmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{vmatrix} = a_{11}a_{22} - a_{12}a_{21}$</p> </div> </div> <p>(3) Order Three: $A = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix}$ $A = \begin{vmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{vmatrix} = a_{11} \begin{vmatrix} a_{22} & a_{23} \\ a_{32} & a_{33} \end{vmatrix} - a_{12} \begin{vmatrix} a_{21} & a_{23} \\ a_{31} & a_{33} \end{vmatrix} + a_{13} \begin{vmatrix} a_{21} & a_{22} \\ a_{31} & a_{32} \end{vmatrix}$</p> <h3 style="text-align: center;">Properties Of Determinants</h3> <div style="background-color: #e0f2f1; padding: 5px; border: 1px solid #ccc; margin-bottom: 10px;"> <p>(1) Property 1: Interchanging rows with columns</p> $\begin{vmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{vmatrix} = \begin{vmatrix} a_1 & b_1 & c_1 \\ a_2 & b_2 & c_2 \\ a_3 & b_3 & c_3 \end{vmatrix}$ </div> <div style="background-color: #e0f2f1; padding: 5px; border: 1px solid #ccc; margin-bottom: 10px;"> <p>(2) Property 2: Interchanging any two rows/ columns</p> $\begin{vmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ c_1 & c_2 & c_3 \end{vmatrix} = - \begin{vmatrix} b_1 & b_2 & b_3 \\ a_1 & a_2 & a_3 \\ c_1 & c_2 & c_3 \end{vmatrix}$ </div> <div style="background-color: #e0f2f1; padding: 5px; border: 1px solid #ccc;"> <p>(3) Property 3: When any two rows/ columns are equal</p> $\begin{vmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \\ b_1 & b_2 & b_3 \end{vmatrix} = 0$ </div> | April 05 Days, May- 05 Days | Through problems based on Matrix and Determinants, they will develop 1)Imagination 2)Systematic approach 3)To handle real life situatio | Students will able to describe Determinant of a square matrix (up to 3 x 3 matrices), minors, co-factors and applications of determinants in finding the area of a triangle. Adjoint and inverse of a square matrix. Solving system of linear equations in two or three variables (having unique solution) using inverse of a matrix. | Students would be able to learn: Determinant of a square matrix (up to 3 x 3 matrices), minors, co-factors and applications of determinants in finding the area of a triangle. Adjoint and inverse of a square matrix. Consistency, inconsistency and number of solutions of system of linear equations by example solving system of linear equations in two or three variables (having unique solution) using inverse of a matrix. |
| 5 | Continuity and Differentiability | May- 08Days, | To enable the students to | Students will be able to learn: Continuity and | Students would be able to learn: |

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| | <div style="text-align: center; margin-bottom: 10px;"> <div style="background-color: red; color: white; padding: 5px; display: inline-block; border-radius: 10px;">Theorems on Continuity and Differentiability</div> </div> <div style="display: flex; justify-content: space-around;"> <div style="background-color: #fff9c4; padding: 10px; border: 1px solid #ccc; width: 45%;"> <p>Rolle's Theorem Let f be a function that satisfies the following three hypothesis:</p> <ol style="list-style-type: none"> f is continuous on the closed interval $[a,b]$. f is differentiable on the open interval (a,b). $f(a) = f(b)$ <p>Then there is a number c in (a,b) such that $f'(c) = 0$.</p> <div style="background-color: #e1bee7; padding: 5px; margin-top: 10px; text-align: center;"> <p>Graphical Representation</p>  </div> </div> <div style="background-color: #fff9c4; padding: 10px; border: 1px solid #ccc; width: 45%;"> <p>The Mean Value Theorem Let f be a function that satisfies the following hypothesis:</p> <ol style="list-style-type: none"> f is continuous on the closed interval $[a,b]$. f is differentiable on the open interval (a,b). <p>Then there is a number c in (a,b) such that</p> $f'(c) = \frac{f(b) - f(a)}{b - a}$ $f(b) - f(a) = f'(c)(b - a)$ <div style="background-color: #e1bee7; padding: 5px; margin-top: 10px; text-align: center;"> <p>Graphical Representation</p>  </div> </div> </div> | <p>June 10 Days</p> | <p>understand 1)Through problems based Rolles Theorem and Mean value Theorem imagination skills are imbibed. 2)Derivatives are used in economics to find out cost function and application skill will developed.</p> | <p>differentiability, chain rule, derivative of inverse trigonometric functions, $\sin x$ and $\cos x$, derivative of implicit functions. Concept of exponential and logarithmic functions. Derivatives of logarithmic and exponential functions. Logarithmic differentiation, derivative of functions expressed in parametric forms. Second order derivatives.</p> | <p>Continuity and differentiability, chain rule, derivative of inverse trigonometric functions, $\sin x$ and $\cos x$, derivative of implicit functions. Concept of exponential and logarithmic functions. Derivatives of logarithmic and exponential functions. Logarithmic differentiation, derivative of functions expressed in parametric forms. Second order derivatives.</p> |
| 6 | <p>Applications of Derivatives</p> | <p>June 08 Days</p> | <p>Through problems based on AOD, they will develop 1)Imagination 2)Systematic approach 3)To handle real life situation</p> | <p>Learners will be able to understand the Applications of derivatives: increasing/decreasing functions, tangents and normal, maxima and minima (first derivative test motivated geometrically and second derivative test given as a provable tool). Simple problems (that illustrate</p> | <p>Students would be able to Understand Applications of derivatives: increasing/decreasing functions, maxima and minima (first derivative test motivated geometrically and second derivative test given as a provable tool). Simple problems (that illustrate</p> |

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| |  | | | <p>basic principles and understanding of the subject as well as real life situations).</p> | <p>basic principles and understanding of the subject as well as real life situations).</p> |
| 7 | Integrals | July-15 Days | <p>Through problems based on integration , they will develop</p> <ol style="list-style-type: none"> 1) Manipulation (assumption) 2) Logical thinking 3) Systematic approach | <p>Understand and appreciate the role of Integration as inverse process of differentiation. Integration of a variety of functions by substitution, by partial fractions and by parts, properties of Definite integrals</p> | <p>Students would be able to:-</p> <ul style="list-style-type: none"> Understand and appreciate the role of Integration as inverse process of differentiation Integration of a variety of functions by substitution, by partial fractions and by parts properties of Definite integrals |

- (i) $\int \frac{dx}{x^2 - a^2} = \frac{1}{2a} \log \left| \frac{x-a}{x+a} \right| + C$
- (ii) $\int \frac{1}{a^2 - x^2} dx = \frac{1}{2a} \log \left| \frac{a+x}{a-x} \right| + C$
- (iii) $\int \frac{dx}{x^2 + a^2} = \frac{1}{a} \tan^{-1} \frac{x}{a} + C$
- (iv) $\int \frac{1}{\sqrt{a^2 - x^2}} dx = \sin^{-1} \frac{x}{a} + C$
- (v) $\int \frac{1}{\sqrt{x^2 - a^2}} dx = \log \left| x + \sqrt{x^2 - a^2} \right| + C$
- (vi) $\int \frac{1}{\sqrt{x^2 + a^2}} dx = \log \left(x + \sqrt{x^2 + a^2} \right) + C$

8 Applications of the Integrals



July-04
Days,
August- 05
Days

To enable the students to develop 1)Critical thinking to visualize shapes 2) Accuracy for calculating area

Students will be able to define Applications in finding the area under simple curves, especially lines, parabolas; area of circles /ellipses (in standard form only) (the region should be clearly identifiable).

Students would be able to define:- Applications in finding the area under simple curves, especially lines, parabolas; area of circles /ellipses (in standard form only) (the region should be clearly identifiable).

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| 9 | Differential Equations | August- 13 Days | To enable the students to understand 1)Different types of solution 2)Different approaches for solution to problem | The students will be able to define Definition, order and degree, general and particular solutions of a differential equation. Solution of differential equations by method of separation of variables, solutions of homogeneous differential equations of first order. | Students would be able to define: Definition, order and degree, general and particular solutions of differential equation. Solution of differential equations by method of separation of variables, solutions of homogeneous differential equations of first order. |
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It is used to solve an equation in which variables can be separated completely.

A differential equation of the form

$$\frac{dy}{dx} + Py = Q \text{ where } P, Q \text{ are constants}$$

or functions of 'x' only is called a First Order Linear Differential Equation and its solution is

$$ye^{\int P \cdot dx} = \int Q \cdot e^{\int P \cdot dx} dx + c.$$

Variable Separation Method

Methods of Solving First Order, First Degree Differential Equations

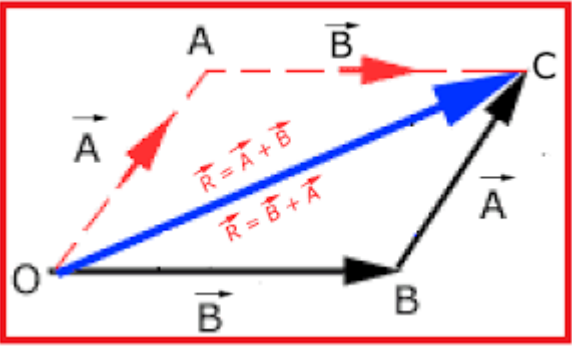
Linear Differential Equations

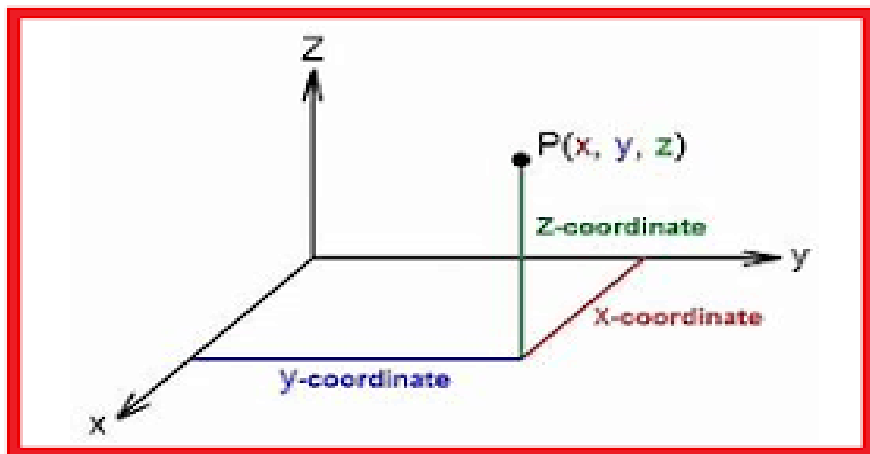
Homogeneous Differential Equations

A differential equation which can be expressed in the form $\frac{dy}{dx} = f(x, y)$ or

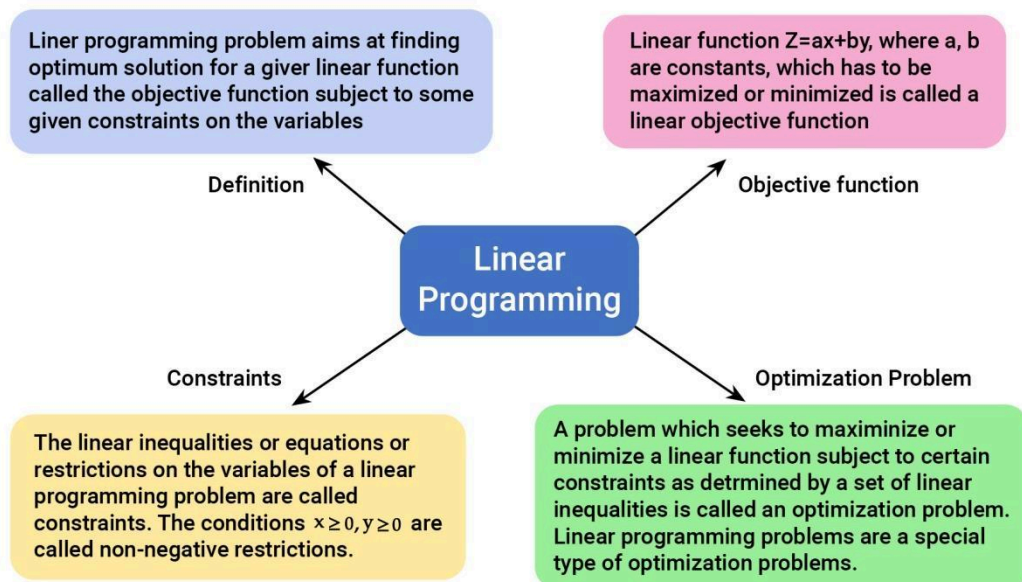
$\frac{dx}{dy} = g(x, y)$ where, $f(x, y)$ and $g(x, y)$ are homogeneous functions is called

a Homogeneous Differential Equation.

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| 10 | <p>Vectors</p>  | September-08 Days | Through the concept of vectors and its usage students will attain 1) Development of visualization 2) understanding need for different types of quantities | Students will be able to Understand the Vectors and scalars, magnitude and direction of a vector. Direction cosines and direction ratios of a vector. Types of vectors (equal, unit, zero, parallel and collinear vectors), position vector of a point, negative of a vector, components of a vector, addition of vectors, multiplication of a vector by a scalar, position vector of a point dividing a line segment in a given ratio. Definition, Geometrical Interpretation, properties and application of scalar (dot) product of vectors, vector (cross) product of vectors | Students would be able to Understand the Vectors and scalars, magnitude and direction of a vector. Direction cosines and direction ratios of a vector. Types of vectors (equal, unit, zero, parallel and collinear vectors), position vector of a point, negative of a vector, components of a vector, addition of vectors, multiplication of a vector by a scalar, position vector of a point dividing a line segment in a given ratio. Definition, Geometrical Interpretation, properties and application of scalar (dot) product of vectors, vector (cross) product of vectors |
| 11 | Three - dimensional Geometry | September-02 Days October-08 Days | Through approach adopted for problems students will attain 1)Imagination 2)Systematic approach 3)Efficiency 4)Creativity | Students will be able to Direction cosines and direction ratios of a line joining two points. Cartesian equation and vector equation of a line, skew lines, shortest distance between two lines. Angle between two lines. | Students would be able to understand Direction cosines and direction ratios of a line joining two points. Cartesian equation and vector equation of a line, skew lines, shortest distance between two lines. Angle between two lines. |



12 Linear Programming



October-10 Days

Through this chapter students will attain
 1) To handle optimization problems (Efficiency)
 2) develop Systematic approach
 3) Differentiate constraint from problem.

Students will be able to Understand Introduction, related terminology such as constraints, objective function, optimization, graphical method of solution for problems in two variables, feasible and infeasible regions (bounded or unbounded), feasible and infeasible solutions, optimal feasible solutions (up to three non-trivial constraints).

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13 Probability

October-06 Days
 November-10 Days

Through this chapter students will develop
 1) Logical thinking

Students will be able to understand Conditional probability, multiplication theorem on

Students would be able to understand Conditional probability, multiplication theorem

Introduction

Probability is the branch of mathematics concerning numerical descriptions of how likely an event is to occur or how likely it is that a proposition is true.

$$\text{Probability} = \frac{\text{Number of Favorable Outcomes}}{\text{Total Number of Outcomes}}$$

Example: Let there be a basket with 3 balls: Red, Green, Blue. If you want to pick a red ball, we can calculate the probability of picking a red ball.

Total number of possibilities = 3

Total number of favorable possibility = 1

Therefore, Probability of getting a red ball = $1/3$



to Handling Risk
2)Imagination for
Manipulating
situation for better
result.

probability, independent
events, total probability,
Bayes' theorem, Random
variable and its probability
distribution, mean of
random variable.

on probability,
independent events
probability, Bayes'
theorem, Random
variable and its
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